

THE NORMAL DISTRIBUTION

- 1 The time taken for all competitors to finish the 50 m freestyle at the school swimming carnival, X seconds, was found to follow a normal distribution where $X \sim N(45, 9)$. Find the following values.
- (a) The time range in which you would expect to find the middle 95% of results.
 - (b) The percentage of students you would expect to take more than 48 seconds.
 - (c) The percentage of students you would expect to take less than 36 seconds.

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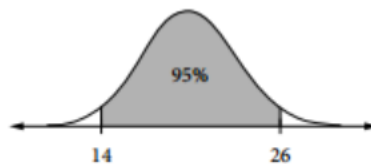
2 $X \sim N(10, 4)$.

- (a) What is the range of x values in which you would expect to find the middle 68%?
- (b) What is the range of x values in which you would expect to find the middle 95%?
- (c) What is the range of x values in which you would expect to find the middle 99.7%?

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- 3 The height X cm of a population is known to be distributed as $X \sim N(170, 81)$.
- (a) What is the percentage of the population expected to be found in the range 152–188 cm?
 - (b) What is the percentage of the population expected to be taller than 197 cm?
 - (c) What is the percentage of the population expected to be shorter than 170 cm?
 - (d) What is the percentage of the population expected to be found in the range 161–197 cm?

- 4 The graph represents a continuous random variable which has a normal distribution.



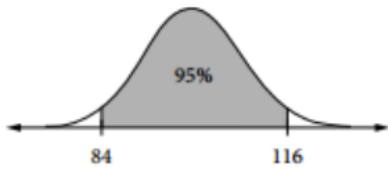
The distribution is best represented by:

- A** $N(14, 26)$ **B** $N(26, 12)$ **C** $N(20, 9)$ **D** $N(20, 3)$

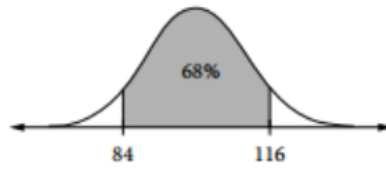
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- 5 Given X is normally distributed with a mean of 100 and a variance of 16, which of the following graphs correctly represents the distribution?

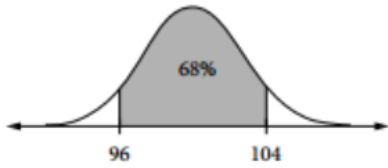
A



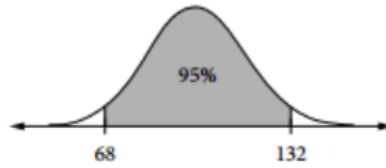
C



B



D



- 6 The marks X obtained by students in an examination were normally distributed with a mean of 85 and a standard deviation of 4. If the top 2.5% of students received a prize, find the minimum whole number score possible to receive a prize.

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- 7 The mass M grams of a batch of commemorative coins is such that $M \sim N(50, 9)$. Each coin is weighed before packaging and will be rejected if its mass is less than 47 g. What is the percentage of coins expected to be rejected?
- 8 Packets of 'Greatstart' breakfast cereal are labelled as having a mass of 500 g. However, the machine that fills the packets actually follows a normal distribution with a mean of 510 g and a standard deviation of 5 g. What percentage of packets, correct to two decimal places, will have a mass less than 500 g?

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12 (a) Using graphing software draw the graph of $f(x) = e^{-x^2}$.

(b) Use Desmos to estimate $\int_{-4}^4 e^{-x^2} dx$

13 (a) Using graphing software, draw the graph of $f(x) = \frac{1}{\sigma\sqrt{2\pi}} e^{-\frac{(x-\mu)^2}{2\sigma^2}}$, for:

(i) $\mu = 10, \sigma = 3$

(ii) $\mu = 0, \sigma = 1$

(b) Use the integration tool in the software to evaluate $\int_{\mu-3\sigma}^{\mu+3\sigma} \frac{1}{\sigma\sqrt{2\pi}} e^{-\frac{(x-\mu)^2}{2\sigma^2}} dx$ in each case in part (a).